## MOLECULAR TENSEGRITY: PREDICTING 1,3- X- - -X DISTANCE IN GAS-PHASE $MX_n$ ( $n \le 4$ ) COMPOUNDS FROM ATOMIC SIZES

Parthasarathy Ganguly

Physical Chemistry Division, National Chemical Laboratory, Homi Bhabha Road, Pune 411008, India RECEIVED DATE (xxx); p.ganguly@ems.ncl.res.in

The Fuller notion<sup>1</sup> of tensegrity structures has structural elements that are held together by compressive and tensile elements that balance each other. Such tensegrity are expected to hold for all length scales, as a general principle. Fuller-Snelson tensegrity structures using (incompressible) struts and (tensile) cables describe well the qualitative features of cell and tissue architecture in complex biological systems<sup>2</sup>. The "molecular tensegrity" that determines, say, the mechanical stability of the structure of isolated gas-phase MX<sub>n</sub> molecules has been elusive. A simplifying feature that we take advantage of is that the energyminimized, density optimized stationary state is consistent with a free-atom-like  $\mu = 0$  condition<sup>3, 4</sup> such that atoms in molecules may be treated independent of each other. Simple mechanical relationships between atomic sizes contribute to interatomic distances that eventually determine the molecular tensegrity structure without requiring to know the (quantum) mechanics of the way the  $\mu = 0$  state is reached from a  $\mu \neq 0$  state.

For an isolated MX<sub>n</sub> molecule, the mutual influences of 1,2bonded (attractive) M-X distance,  $d_{M-X}$ , and 1,3- non-bonded (repulsive) X- - -X distances,  $d_{X-X}$ , is expressed (eqn 3) as a tensegrity factor (similar to the tolerance factor in solids<sup>7, 8</sup>) that forms the quantitative basis for molecular tensegrity. 1,2interatomic distance,  $d_{MX}$ <sup>n0</sup>, have been expressed as<sup>3, 5</sup> an universal function of "core" (small compared to interatomic distances) empirical<sup>5</sup> atomic sizes,  $r_G$  as

 $d_{MX}^{n0} = CR_0^+(M)/F_S(M) + CR_0^-(X)$ 

 $= [C_0^{+}r_G(\mathbf{M}) + D_0^{+}]/F_S(\mathbf{M}) + C_0^{-}r_G(\mathbf{X}) + D_0^{-}$ (1)

with  $CR_0^{\pm} = C^{\pm}r_G + D_0^{\pm}$ , and  $C_0^+ = 2.24$ ,  $C_0^- = 2.49$ ,  $D_0^- = 111$  pm and  $D_0^+ = -37$  pm. The term<sup>9</sup> F<sub>S</sub>(M) = 1 ( $n_v = 0$ ) for all M except for transition metal MX<sub>3</sub> ( $n_v = 1$ ) and MX<sub>4</sub> compounds ( $n_v = 2$ ). The superscript,  $\pm$ , refers to charge-transfer states  $CR_0^+$  and  $CR_0^-$  in eqn 1. The size  $CR_0^-(X)$  is close to the ionic radii in solids<sup>5</sup> and is different from the van der Waals' radius<sup>10</sup>,  $r_{VDW} \neq CR_0^-(X)$ . The non-bonded distance,  $d_{XX}^{00}$  is expected to be

$$d_{XX}^{00} = 2 \text{K} C R_0^{-}(\text{X})$$
(2)

Unless otherwise mentioned, we take 
$$K = 1$$
 hereafter. Eqns 1 and 2 are required to define an ideal "tensegrity" factor<sup>10</sup>,  $t_{n0}^{\pm}$ , as  $t_{n0}^{\pm} = d_{MX}^{n0}/d_{XX}^{00}$  (3)

We now express an experimental quantity  $F_{S}(obs)$  as

F<sub>s</sub>(obs) =  $d_{XX}(obs)/d_{XX}^{00} \equiv d_{XX}(obs)/2CR_0^{-1}(X)$  (4) A plot of F<sub>s</sub>(obs) vs  $t_{n0}^{\pm}$  (Figure 1) for all gas-phase MX<sub>2</sub>, MX<sub>3</sub> and MX<sub>4</sub> compounds<sup>11, 12</sup> (X = atom of insulating element) two nearly linear relationships of the type

$$F_{\mathcal{S}}(\text{obs}) = \mathbf{A} - \mathbf{B}t_{n0}^{\pm} \tag{5}$$

are obtained (Fig 1) which we refer to as Type I and Type II. In general ,Type I  $MX_n$  compounds have M = atom of s-block metal, (met(s) in Figure 1), or transition metal dihalides (TM(n = 2)), while Type II compounds have M as an atom of an insulating element (ins), *p*-block metal (met(p)) or transition metal  $MX_3$  or

MX<sub>4</sub> compounds (TM(n > 2)). The compounds BH<sub>2</sub>, AlH<sub>2</sub>, MH<sub>4</sub> (M = Si, Ge, Sn and Pb) and SeO<sub>3</sub> are better described as type I compounds. From the ratios of the two slopes in Fig 1 we find  $F_{S}(\text{obs})^{(\text{II})}/F_{S}(\text{obs})^{(\text{II})} \sim 1.12$  for the same  $t_{n0}^{\pm}$ .

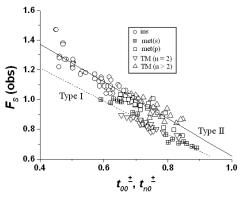


Figure 1. Plot of  $F_S(\text{obs})$  (eqn 4) vs the tolerance factor,  $t_{n0}^{\pm}$  (eqn 3) for gas-phase MX<sub>2</sub>, MX<sub>3</sub> and MX<sub>4</sub> compounds. Dotted line: Type I compounds;  $F_S(\text{obs}) = 1.66(0.04)t_{00}^{\pm} - 1.12(0.5)$ ; R = -0.96, SD = 0.03. Full line: Type II compounds,  $F_S(\text{obs}) = 1.87(0.02)t_{00}^{\pm} - 1.25(0.4)$ ; R = -0.96, SD = 0.04.

The linear relationships in Figure 1 may be understood from Fuller's original description<sup>1</sup> of tensegrity which considers "continuous, tensional behaviours" as in a stretched membrane of a filled balloon. The "critical proximities that show up physically" are "repellings" which keep the molecular network constituting the balloon membrane stretched outwardly in all directions. The geometrically simplifying Fuller feature of the balloon membrane is the notion of "paired oppositely accelerated molecules" caroming around in "most comfortable great circles", three of which intersect to give vertices of two spherical octahedral, one octaehdron for each opposing direction. The linear relationships (eqn 5) in Figure 1 is understood from the geometrical limits of octahedral structures.

We examine eqn 4 in terms of the ratio of atomic sizes,  $(CR_0^+(M)/CR_0^-(X))$ . The ratio  $CR_s^+(M)/CR_s^-(X) = 0.414$ , geometrically represents the lower limit for stable octahedral coordination in ligand close-packed scenarios quite different from that envisaged by Gillespie *et al*<sup>13, 14</sup>. Writing eqn 3 as  $t_{00}^{\pm} \equiv 0.5(CR_0^+(M)/CR_0^-(X) + 1)$  we require from eqn 5  $F_s(\text{obs}) = 1$ when  $t_{00}^{\pm} = 1/1.414 = 0.707$  as in the fit for type II compounds in Figure 1. Ideally, we prefer  $F_s(\text{obs}) = (2 - 1.414t_{00}^{\pm})$  and obtain ( $\kappa$ = effective dielectric constant, see eqn 7) from eqns 2, 3 and 5

 $d_{XX}(\text{calcd}) = 2\kappa K C R_0^{-}(X)/(2 - 1.414 t_{00}^{\pm})$  (6) as an "*ab initio*" quantity dependent only on "portable"<sup>15</sup> core atomic size of M and X atoms (eqn 1). The best fits to plots of

 $d_{XX}$ (obs) vs  $d_{XX}$ (calcd) ( $\kappa = 1$  in eqn 6) in more than 160 gas-phase MX<sub>2</sub>, MX<sub>3</sub> and MX<sub>4</sub> compounds give (R > 0.99)  $d_{XX}$ (obs) =  $1.19d_{XX}$ (cal) -15.8(9.2) for type I compounds and  $d_{XX}$ (obs) =  $1.04d_{XX}$ (cal) -6.7 for Type II compounds. The improvement in the R factor of the fits as compared to that in Figure 1 attests to the goodness of the model (eqn 6), especially considering that the gas-phase distances are obtained at various conditions of measurement, temperature and pressure and without a substantial theoretical basis for the "core" atomic sizes.

The finite intercepts of the best fits using eqn 6 highlights the uncertainty in the way the effective dielectric constant,  $\kappa$ , of eqn 6 varies with atomic size (as it should because of changes in polarizability with size). We have varied  $\kappa$  as  $\kappa = 1 + (Ld_{MX}^{00})^2$ such that the intercept of the best fit is zero. We find that L  $\sim$ 0.001 (for  $d_{MX}^{00}$  in pm) is empirically required for all compounds We thus write

 $d_{XX}(\text{calcd}) = 2\{1 + (0.001d_{MX}^{00})^2\} \text{K}CR_0^{-}(X)/(2 - 1.414t_{00}^{\pm})$ (7) The best fits to plots of  $d_{XX}(obs)$  vs  $d_{XX}(calcd)$  using eqn 7 then requires with K(Type I)/K(Type (II)  $\approx 1.08$  (Fig 2). The standard deviation is 8 pm for type II and 13 pm for type I which is comparable to calculated values<sup>11</sup> employing latest theoretical methodologies

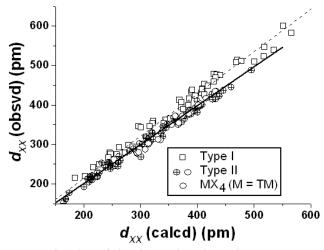
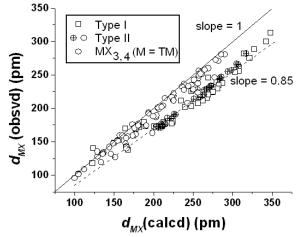


Figure 2. Plots of  $d_{XX}(obs)$  vs  $d_{XX}(calcd)$  using eqn 7 (except transition metal tetrahalides for which we take  $\kappa = 1$ ). The best fits (R > 0.993) give  $d_{XX}(obs)$  vs 1.07 $d_{XX}(calcd)$  for type I compounds and  $d_{XX}(obs) vs 0.99 d_{XX}(calcd)$  for type II compounds

The size  $2CR_0(X)$  (K = 1 in eqn 2) is close to the negatively charged ionic radii of atoms in solids while the size  $2*1.08*CR_0^{-1}$ (X) (K = 1.08 in eqn 2) could be close to the so-called van der Waals' radii<sup>10</sup>,  $r_{VDW}$ . For example, the ratio of the Bondi radii<sup>10</sup> of  $r_{VDW}$  for C, N, O, F to the corresponding values of  $CR_0(X)$  is close to 1.09. The nearest-neighbour interatomic separation of Ne, Ar, Kr and Xe in their crystals<sup>18</sup> when given by  $2*1.08*CR_0(X)$ could require  $r_G$  values of 0.27, 0.51, 0.61 and 0.74 (a. u.), respectively, which is close to that expected (e.g., from the Zunger-Cohen valence s-electron radii<sup>6</sup> of 0.22, 0.46, 0.65 and 0.75 (a. u.)).

A point of importance is the relative insensitivity of nonbonded X- - -X distances to the deviation (Fig 3) of bonded M-X distances from the calculated value of  $d_{MX}^{n0}$  (using eqn 1). This is consistent with early seminal observations of Bartell<sup>16</sup>, reemphasized by Gillespie and coworkers<sup>13, 14</sup>. The invariance of 1,3- non-bonded distances may be regarded as struts and the more variable 1.2- distances as tensile elements in molecular tensegrity structures of gas-phase  $MX_n$  compounds. Our methodology is

applicable to terminal linkages in gas-phase dimers (such as those in  $M_2X_6$  dimers, M = Al, Ga, X = halogen) or organic compounds but not to the bridged linkages (showing effects due to a transition to a condensed state). The main exceptions (not shown) are the linear compounds KrF<sub>2</sub> and XeF<sub>2</sub> (not shown) and the axial nonbonded F- - -F distances in T-shaped molecules, BrF3 and ClF3. The understanding of non-bonded X---X distance using eqn 5 for these and other n > 4 MX<sub>n</sub> compounds requires more elaboration.



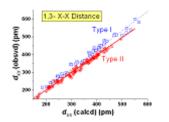
*Figure 3.* Plots of  $d_{MX}(\text{obs})$  of gas-phase MX<sub>n</sub> compounds  $(n \ge 4)$ (Refs 11, 12) versus  $d_{MX}^{n0}$  (calculated) using eqn 1.

In conclusion, we find that molecular tensegrity seems to be a powerful concept for molecular structure. Our methodology does not require prior knowledge of ionic character of M-X bond, nor the full weight of quantum chemical compliculations, given a core atomic size.

The author thanks the Council of Scientific and Indusrial Research for an emeritus sustenance grant.

Supporting Information Available: Table of observed and calculated distances for ~ 160 gas-phase  $MX_n$  compounds, a figure showing the naure of fit obtained from eqn 6..

- 1. (a) Fuller, R.B., 1975. Synergetics, Explorations in the Geometry of Thinking. Collier Macmillan, London, UK. (b) Letter written by Buckminster Fuller to Robert Burhardt dating from February 2 to March 18, 1982 and found on the web site of the Buckminster Fuller Institute (www.bfi.org).
- 2002, 108, 134 and references therein
- Gangul, P., J. Am. Chem. Soc., 1995, 117, 1677
   see Zunger, A., Phys. Rev. B, 1980, 20, 5839 and references therein.
- Goldschmidt's tolerance factor in MBX<sub>3</sub> perovskites is given as  $t = d_{MX} \sqrt{2} d_{BX} \equiv d_{MX} / d_{XX}$ ; see Ganguly, P. and Shah, N., *Physica C*, **1993**, 208, 307 and references therein
- 8. see Simon, A, Angew. Chem. 1983, 95, 94-113 [Int. Ed. Engl. 1983, 22, 95-1131
- 9. See Ganguly, P., J. Am. Chem. Soc., **1995**, 117, 2656. For  $n_v$  "unsaturated" (we prefer the term "extrabonding") valence electrons  $F_S \approx [1 + (2\pi v)^2 \{S(S+1)\}^{1/3}] \approx 1, 1.18, 1.26, 1.32, 1.38 an 1.46 for <math>n_v = 0, 1, 2, 3, 4$ and 5, respectively.
- 10. see, for example, Bondi, A., J. Phys. Chem., 1964, 68, 441-451
- 11. see Hargittai, M., Chem. Rev. 2000, 100, 2233-2301 and references therein for a comprehensive review.
- 12. Interatomic distances are obtained from CRC Handbook of Chemistry and *Physics*, 61st ed., Weast, R. C., Ed.; CRC Press: Boca Raton, 1980; F-221 13. Gillespie, R. J., Robinson, E. A., *Chem. Soc. Rev.*, **2005**, *34*, 396–407
- 14. see Robinson, E. A., and Gillespie, R. J., Inorg. Chem. 2003, 42, 3865-3872:
- 15. Hoffmann, R., J. Mol. Struct. (Theochem.), 1998, 424, 1
- see Bartell, L. S., *Coord. Chem. Rev.*, 2000, 197, 37
   see Wyckoff, R. W. G., "Crystal Structure", 2<sup>nd</sup> Edition, Vol 1., Chapter II, Interscience Publishers, 1964



ABSTRACT This article describes a methodology for obtaining quantitatively the 1,3-non bonded distances in gas-phase  $MX_n$  compounds ( $n \le 4$ ) of nearly 160 inorganic compounds (including those of transition metal elements). The simple principles behind its methodology (involving only linear equations), its quantitative character, its transparency, its portability and its generality have not been noticed before. There is no dependence on the "ionic character" of the M-X bond, nor on complex calculations using molecular wave functions, once the atomic size is given.